

Justify It!

**A growing list of mathematical
reasons to justify your work.**

Commutative Property

of Addition

$$a+b=b+a$$

$$2+3 = 3+2$$

of Multiplication

$$a \cdot b = b \cdot a$$

$$2 \cdot 3 = 3 \cdot 2$$

Associative Property

of Addition

$$(a+b)+c=a+(b+c)$$

$$(2+3)+4 = 2+(3+4)$$

of Multiplication

$$(a \cdot b) \cdot c = a \cdot (b \cdot c)$$

$$(2 \cdot 3) \cdot 4 = 2 \cdot (3 \cdot 4)$$

Identity Property

of Addition

$$a + 0 = a$$

$$2 + 0 = 2$$

of Multiplication

$$a \cdot 1 = a$$

$$2 \cdot 1 = 2$$

Inverse Property

of Addition

$$a + (-a) = 0$$

$$2 + (-2) = 0$$

of Multiplication

$$a \cdot \frac{1}{a} = 1$$

$$2 \cdot \frac{1}{2} = 1$$

Symmetric POE

If $a=b$, then $b=a$.

If $x=2$, then $2=x$.

Reflexive POE

$a=a$

A number is always equal to itself.

Transitive POE

If $a=b$ and $b=c$, then $a=c$.

If $x=2$ and $2=y$, then $x=y$.

Distributive POE

$$a(b+c) = ab+ac$$

$$2(x+3) = 2x+6$$

Addition POE

If $a=b$, then $a+c=b+c$.

If $x=2$, then $x+3=2+3 \rightarrow x=5$

Subtraction POE

If $a=b$, then $a-c=b-c$.

If $x=2$, then $x-3=2-3 \rightarrow x=-1$

Multiplication POE

If $a=b$, then $a \cdot c = b \cdot c$.

If $x=2$, then $x \cdot 4 = 2 \cdot 4$.

Division POE

If $a=b$, then $a \div c = b \div c$

If $x=2$, then $x \div 4 = 2 \div 4 \rightarrow x = \frac{1}{2}$.

Substitution POE

If $a=b$, then b can replace a .

If $x=2$, then $x+5=2+5 \rightarrow x+5=7$

Zero Product Property

If $a \cdot b=0$, then $a=0$ and/or $b=0$

If $(x-2)(x+3)=0$, then $x-2=0$ and/or $x+3=0$

Blank POE

If , then .

If, then .

Blank POE

If , then .

If, then .